

NTNU

Innovation and Creativity

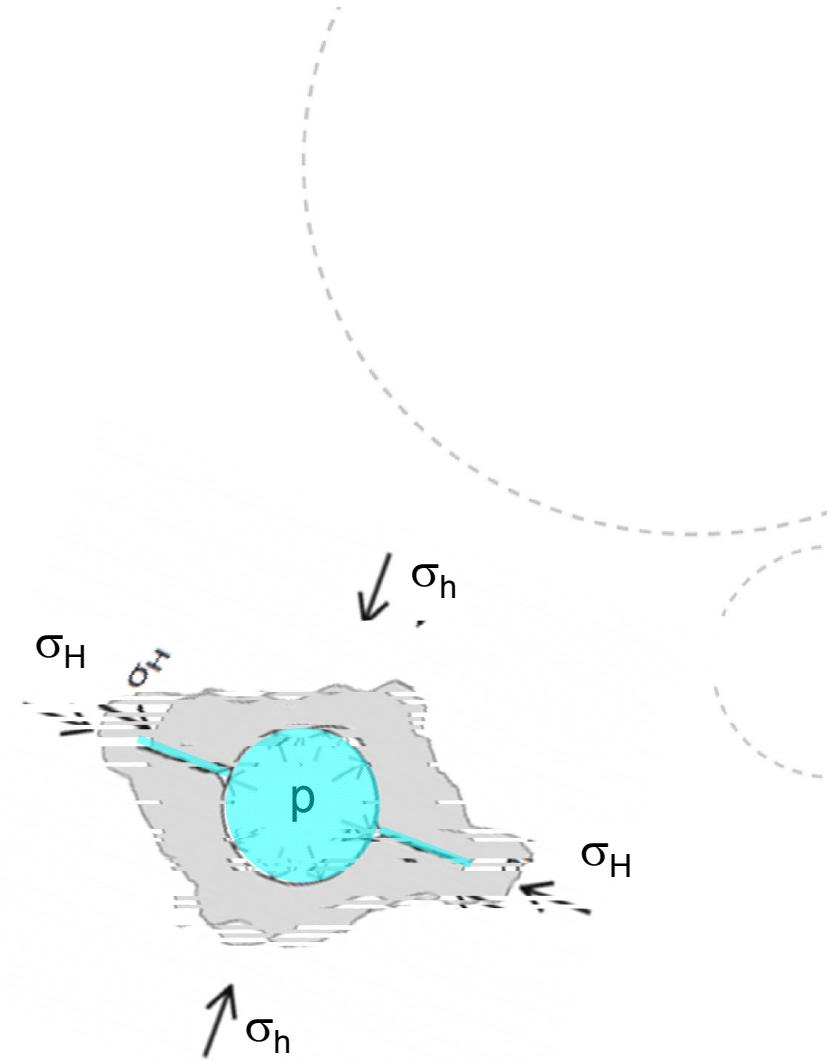
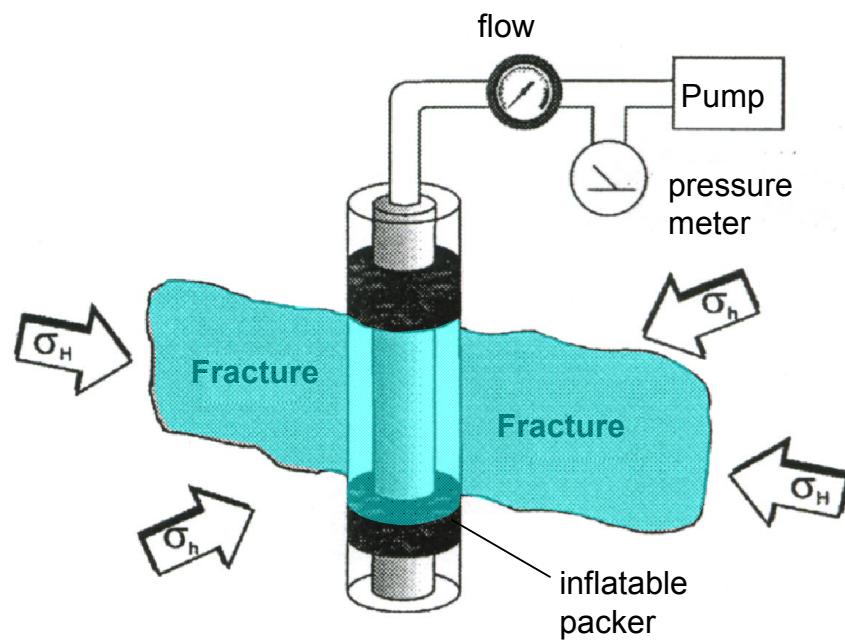
Teoretisk Grunnlag for Hydraulisk Splitting

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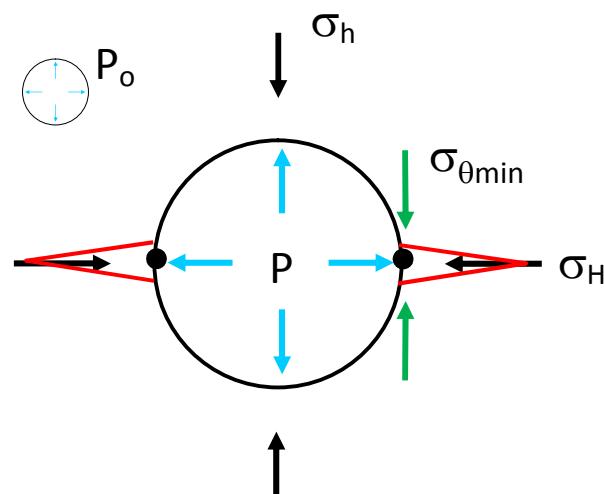
Prinsippet



Antagelser

- Materialet:
 - lineært elastisk,
 - isotropisk,
 - homogent
- Insitu spenningsforhold:
 - ikke-hydrostatisk spenningstilstand
 - en av de tre hovedspenningene er parallel med borehullet

Teorier



σ_t = Strekkfasthet

P_o = Poretrykket

P = Vanntrykket i borehullet

P_c = Splittingstrykket

Minste tangentialspenning:

Uten vanntrykket i borehullet:

$$\sigma_{\theta\min} = 3\sigma_h - \sigma_H + P_o$$

Med vanntrykket:

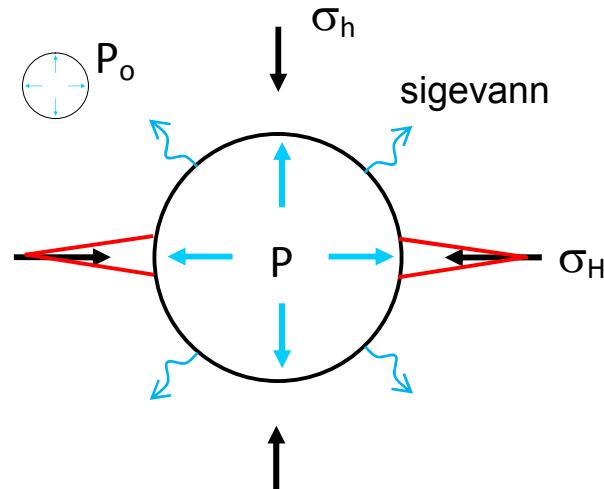
$$\sigma_{\theta\min} = 3\sigma_h - \sigma_H + P_o - P$$

Strekkbrudd :

$$\sigma_{\theta\min} = 3\sigma_h - \sigma_H + P_o - P_c = -\sigma_t$$

$$P_c = \sigma_t + 3\sigma_h - \sigma_H + P_o$$

I permeabelt berg:



$$P_c = \frac{\sigma_t + 3\sigma_h - \sigma_H + 2\eta P_o}{2(1-\eta)}$$

$$\eta = \frac{\alpha(1-2\nu)}{2(1-\nu)}, \text{ poreelastisk koeffisient}$$

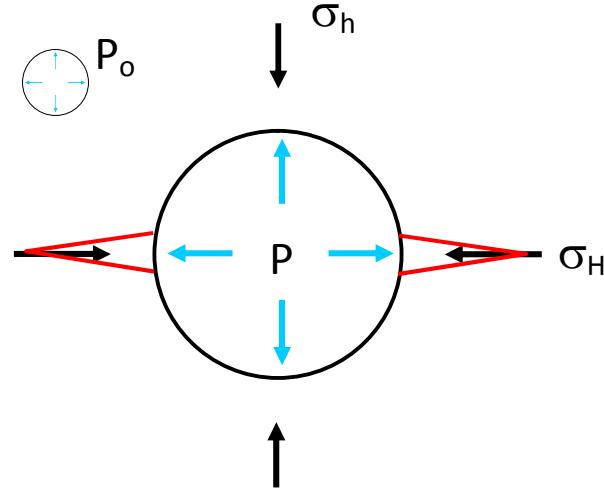
$$\alpha = 1 - K/K_s, \text{ Biot koeffisient}$$

ν = Poissons tall

K = Bulkmodul av berg (korn + porer + sprekker)

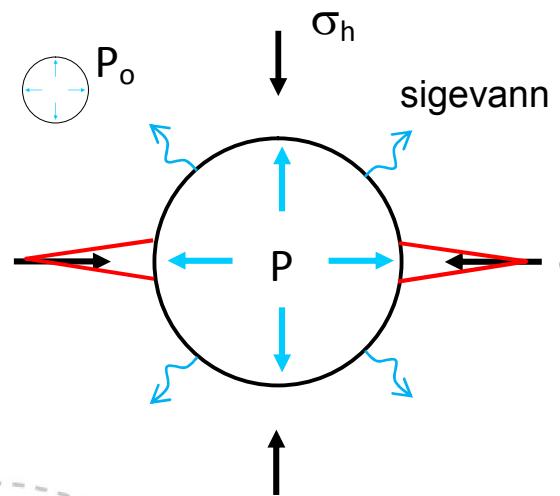
K_s = Bulkmodul av mineralkorn

Beregningsligninger



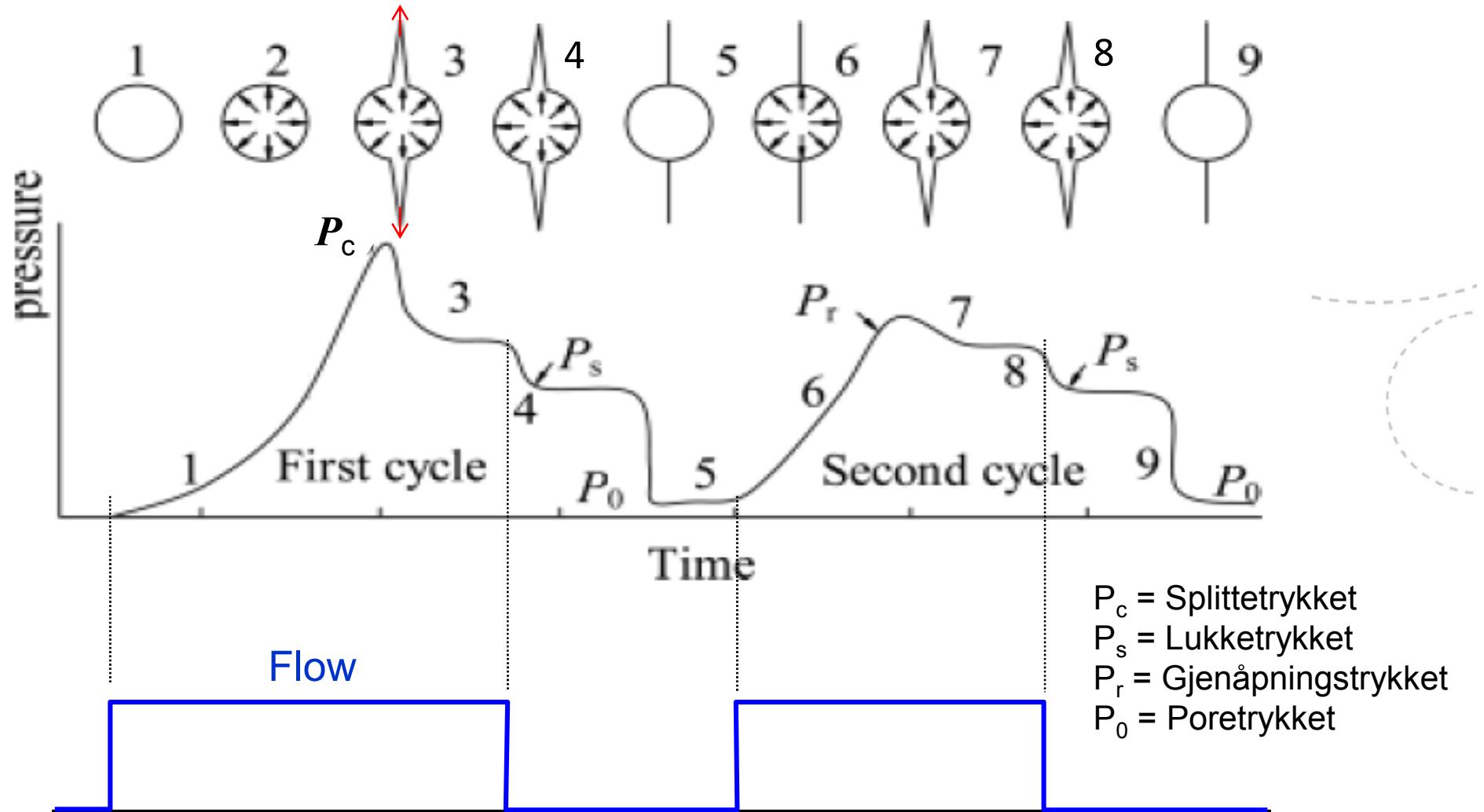
Når vann er ikke penetrerende:

$$P_c = \sigma_t + 3\sigma_h - \sigma_H + P_o \quad (1)$$



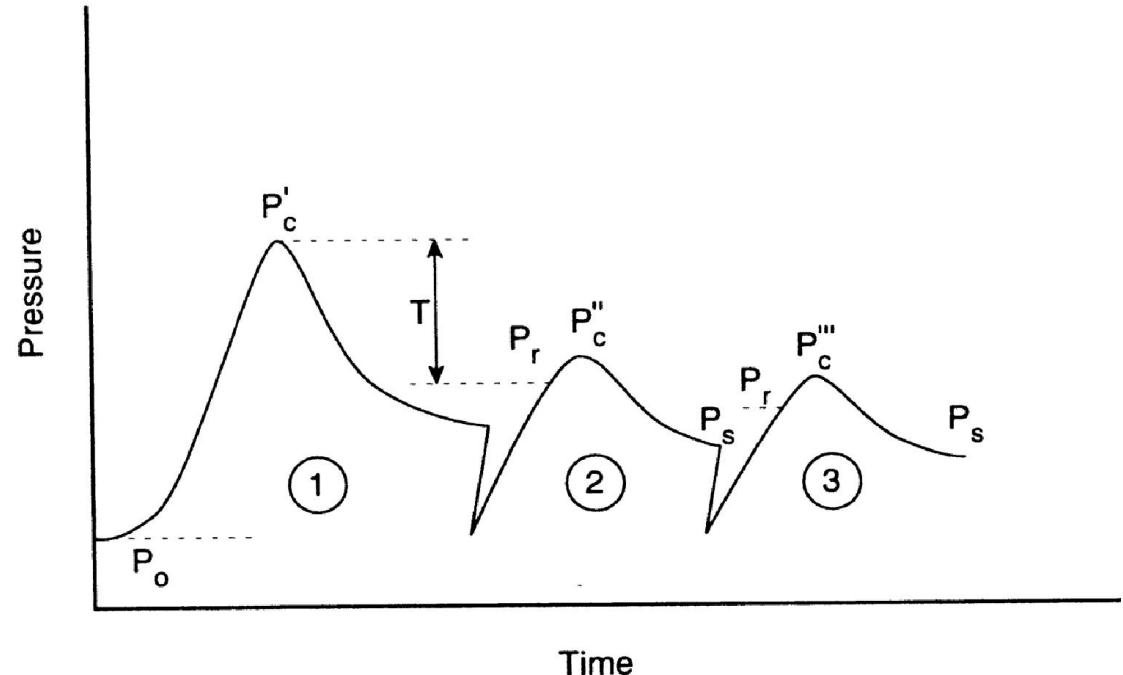
Når vann er penetrerende:

$$P_c = \frac{\sigma_t + 3\sigma_h - \sigma_H + 2\eta P_o}{2(1-\eta)} \quad (2)$$



Strekkfashet:

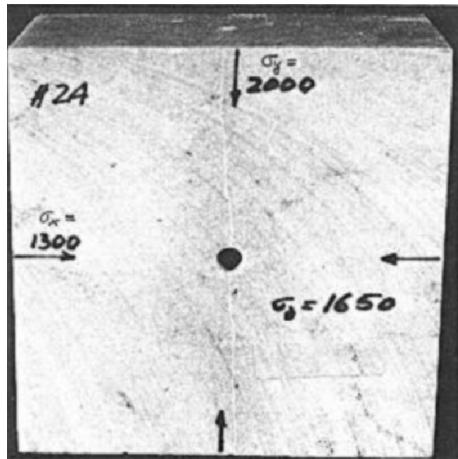
$$\sigma_t = P_c' - P_r$$



Gjenåpningstrykket P_r er det punkt hvor en plutselig nedgang i trykkøkning med tiden

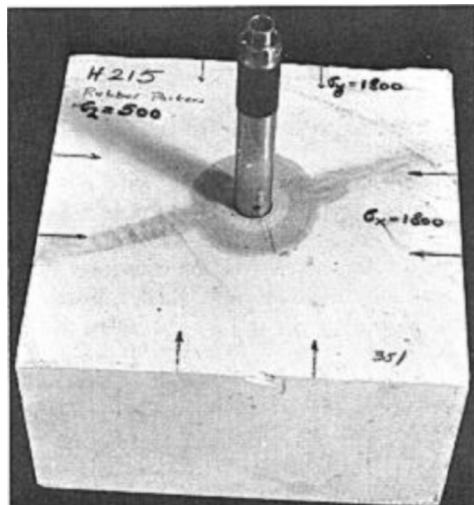
Bruddtyper (i et vertikalt borehull)

- Sprekken er vertikal, $\sigma_h = \sigma_3$
- Sprekken er horisontal, $\sigma_v = \sigma_3 \ll \sigma_h$
- Sprekken initiert vertikalt men utvider sig horisontalt,
 $\sigma_v = \sigma_3$

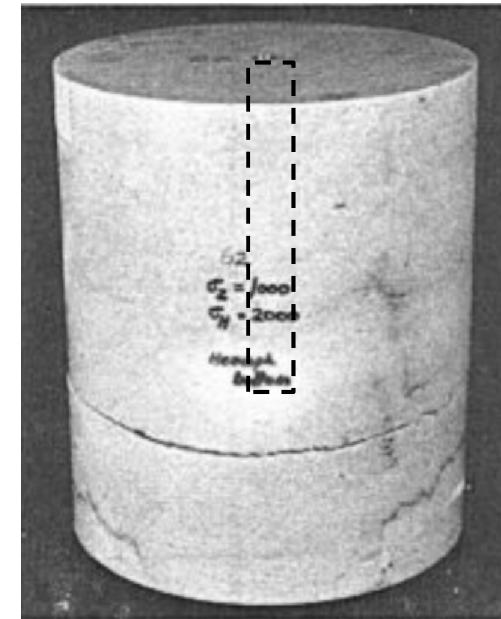


Tennessee marmor

Vertikalsprekk, $\sigma_x < \sigma_z < \sigma_y$



Vertikalsprekk, $\sigma_z < \sigma_x = \sigma_y$

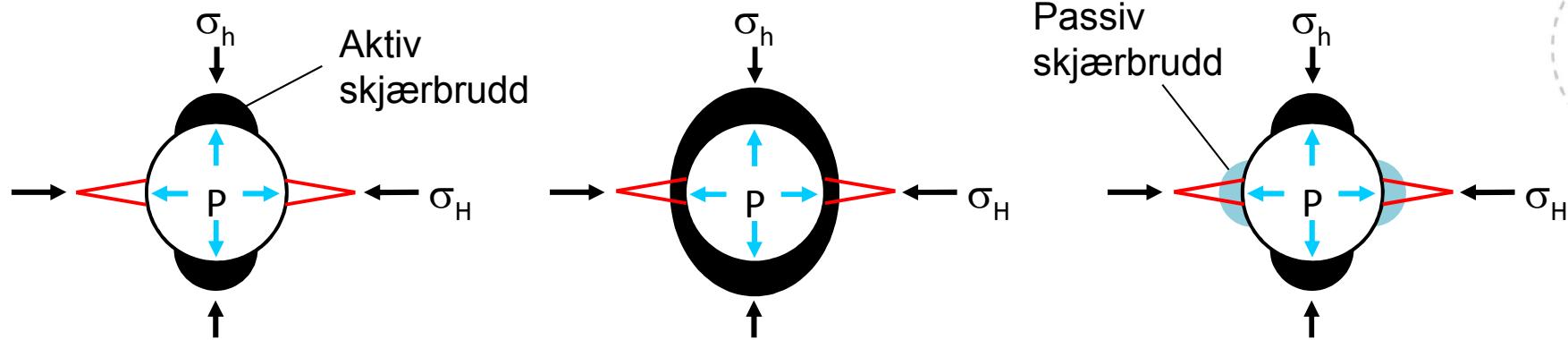


Horisontalsprekk
 $\sigma_z < \sigma_x = \sigma_y$

(Haimson & Fairhurst 1969)

Splittingtrykket i svakt berg

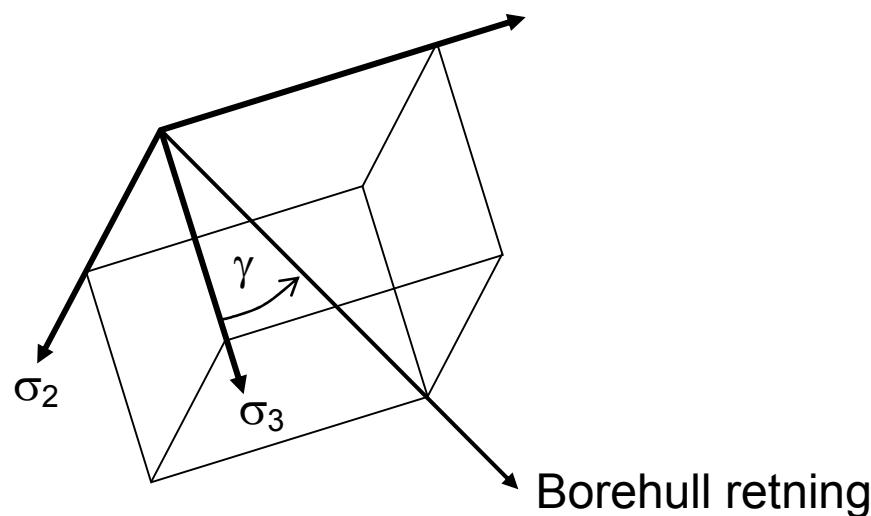
- Svakt berg er karakterisert av lav fasthet
- Skjærbrudd kan forekomme like etter hullboring og under trykking



Skjærbrudd endrer spenningsfordelingen rundt hullet
så at ligningene (1) og (2) ikke er gyldig

Borehull ikke i retning av hovedsspenningene

$$P_c = \sigma_t + 3\sigma_h - \sigma_H \cos^2 \gamma - \sigma_v \sin^2 \gamma + P_o$$



Fire ukjente: $\sigma_1, \sigma_2, \sigma_3, \gamma$

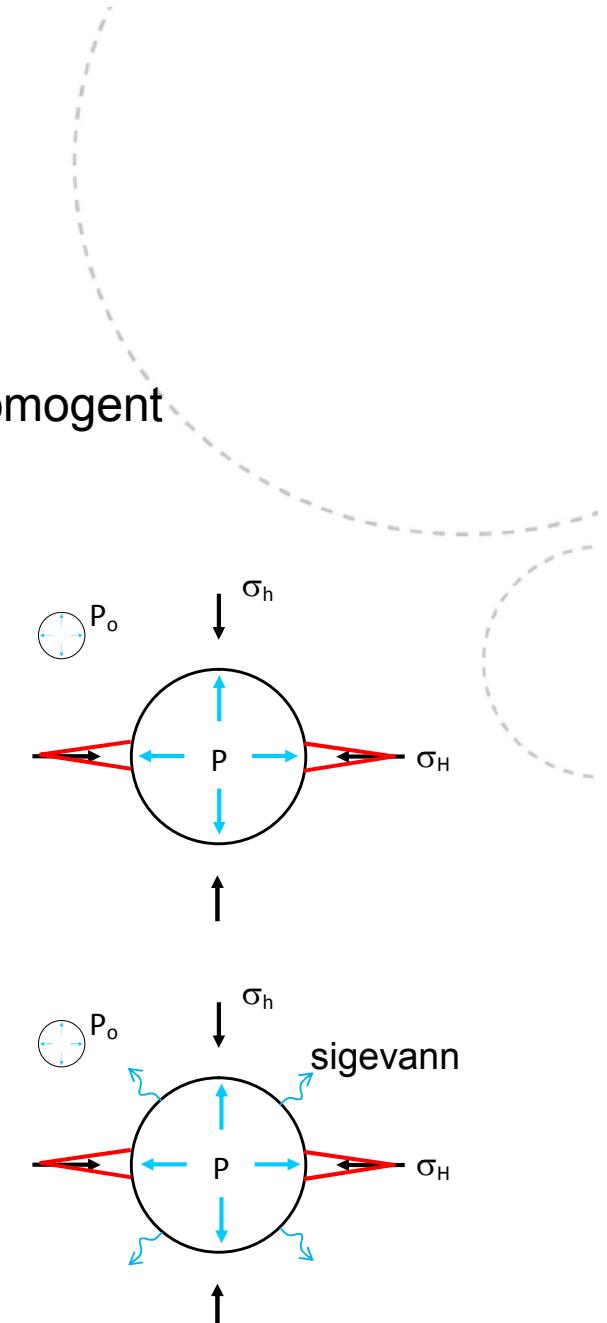
Hvem har prøvd metoden?

Oppsummering

- Antagelser
 - Materialet er lineært elastisk, isotropisk og homogent
 - $\sigma_H > \sigma_h$ og σ_v parallel med borehullet
- Beregningslingninger:

$$P_c = \sigma_t + 3\sigma_h - \sigma_H + P_o \quad (1)$$

$$P_c = \frac{\sigma_t + 3\sigma_h - \sigma_H + 2\eta P_o}{2(1-\eta)} \quad (2)$$



Referanser

- Amadei B. and Stephansson, O. 1997. Rock Stress and Its Measurements. Chapman & Hall.
- Haimson, B. and Fairhurst, C. 1969. In-situ stress determination at great depth by means of hydraulic fracturing. 11th US Symp. Rock Mech., Chapter 28, 559-584.
- Zoback, M.D., Rummel, F., Jung, R. and Raleigh, C.B. 1977. Laboratory hydraulic fracturing experiments in intact and pre-fractured rock. Int J of Rock Mech Min Sci & Geomech Abstr, 14, 49-58.